

# Pattern Classification using Rectified Nearest Feature Line Segment



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# Pattern classifiers

## e Nearest Neighbor (NN)

- T.M. Cover and P.E. Hart, 1967

- Simplest
- Effective
- Most popular

## e The proposed method : RNFLS

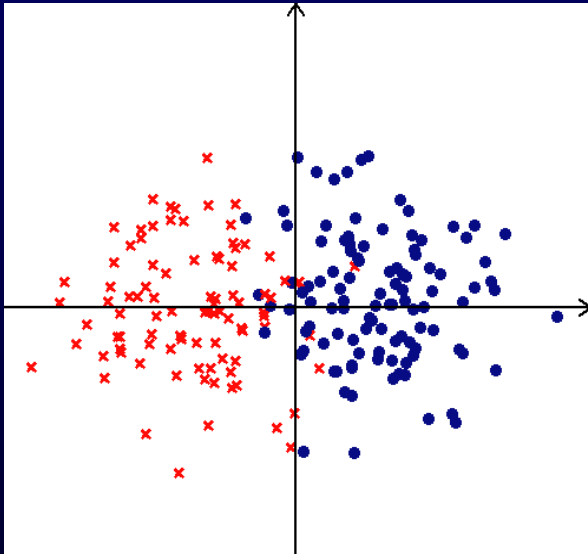
- A classifier to improve NN
- by an average of 3% correct classification rate



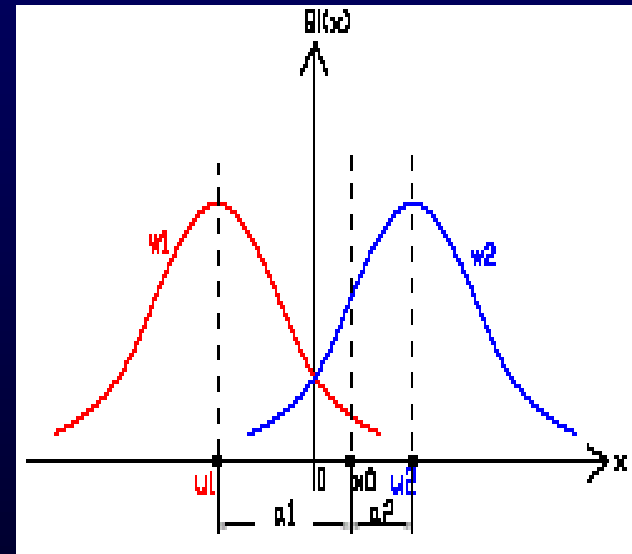
**3% UP**

# Problem of Nearest Neighbor

- ⓐ Risks occur in the intersection area



Sample Distribution

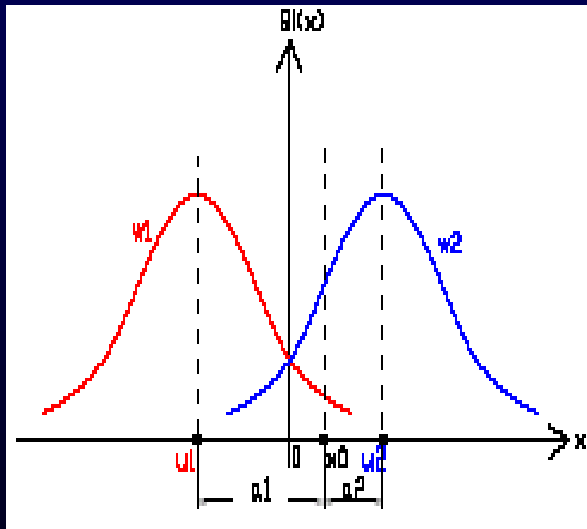


Density Function

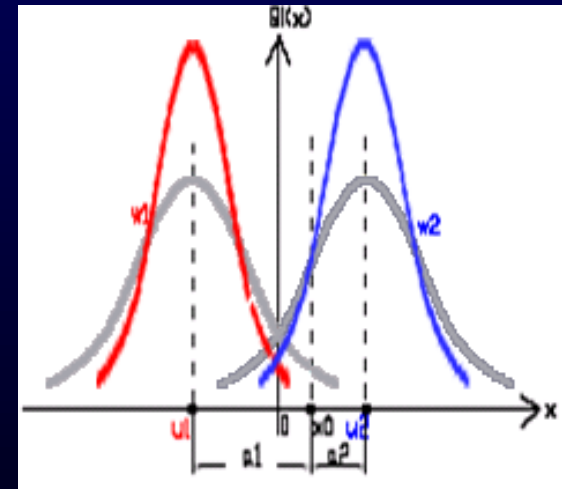
# Motivation : Centralization

- e How to improve NN in the intersection area?

Centralizing the density function



Centralizing



# History: 'Feature Line'

④ From **NN** -> **NFL** -> **RNFLS**

⊛ Nearest Neighbor (**NN**)

- T.M. Cover and P.E. Hart, 1967

⊛ Nearest Feature Line (**NFL**)

- S.Z. Li and J. Lu, 1999

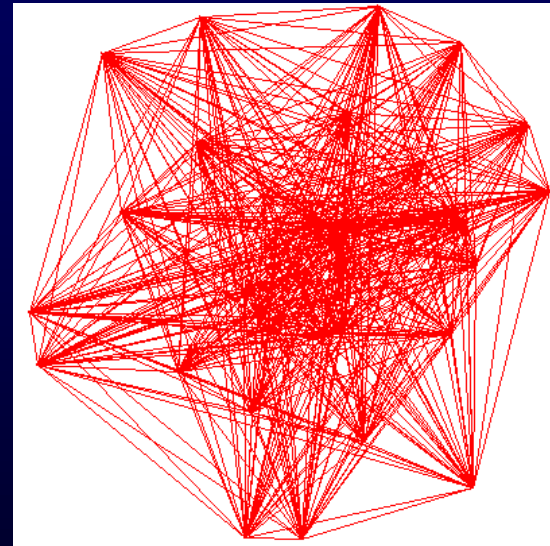
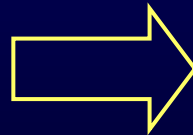
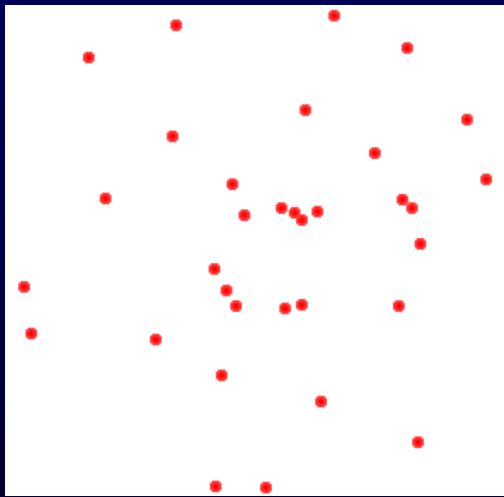
⊛ Rectified-NFL-Segment (**RNFLS**)

- H. Du and Y.Q. Chen, this Paper

④ **NFL & RNFLS** support the original sample points to improve **NN** classifier

# The Method (1/2)

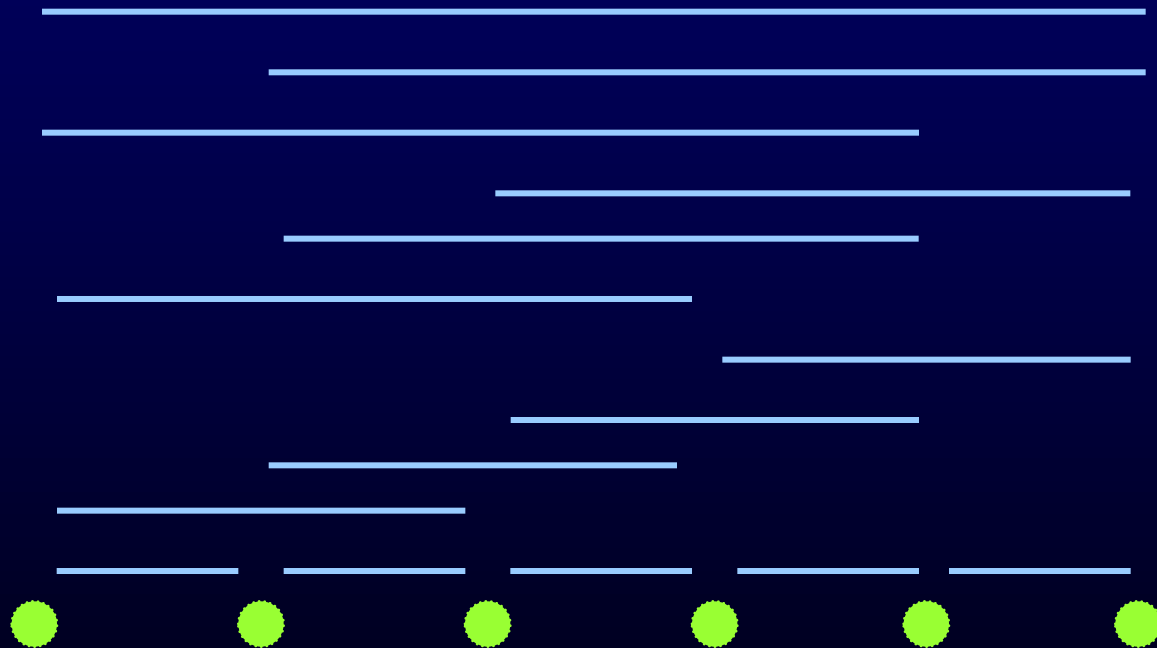
- Using line segments connect each pair of samples from one class



- Feature Line Segments** support the original samples

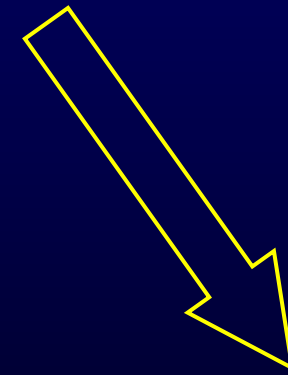
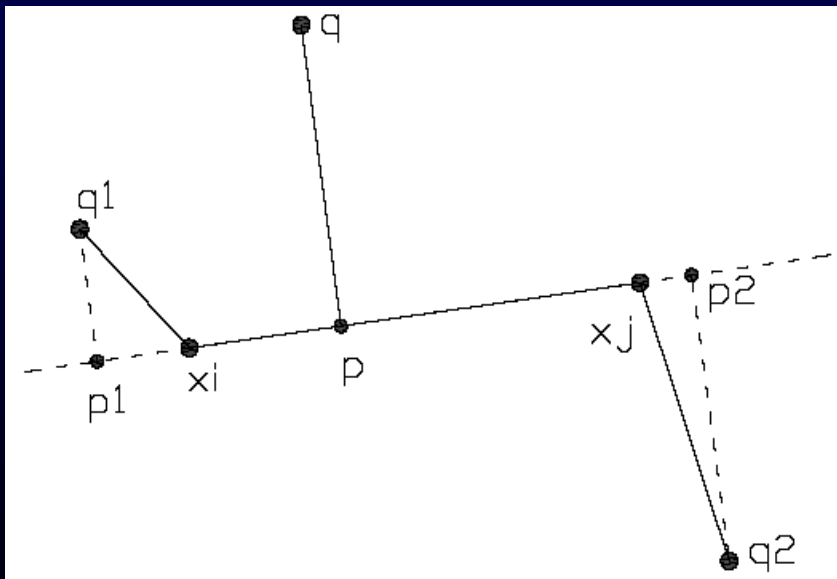
# Why it works?

## @ 1D – example



# The Method (2/2)

- Distance metric:
  - classifying by finding out the **Nearest Feature Line Segment** to the query point

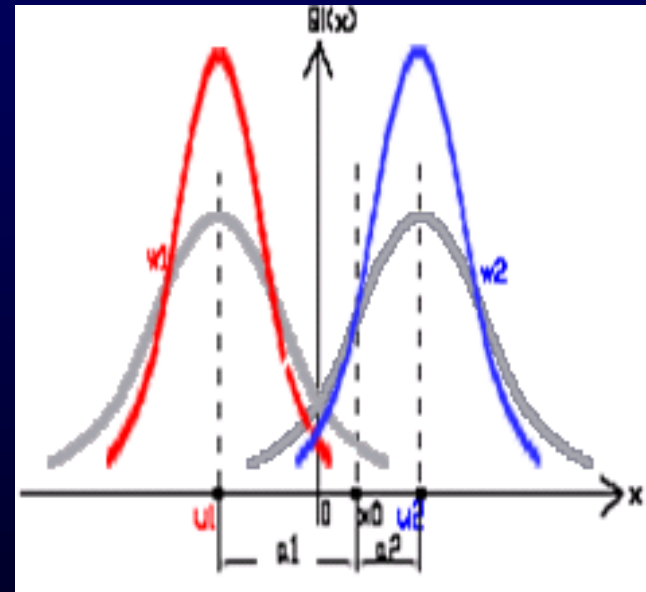
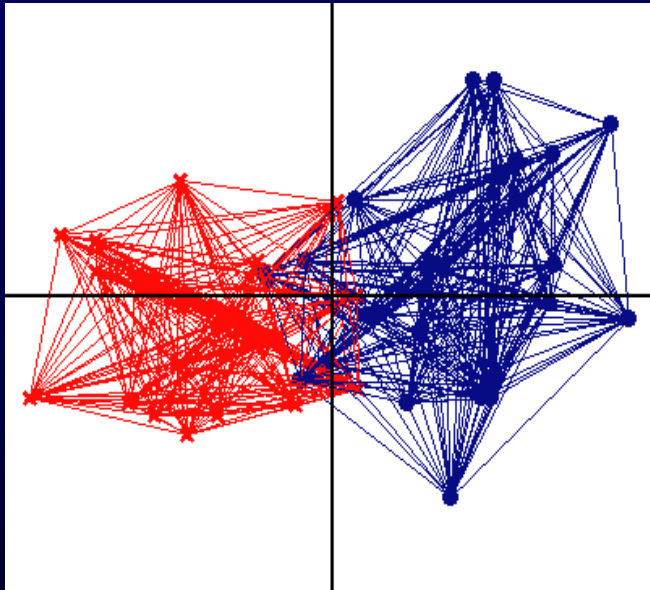


**NFL-Segment**



# Two-Gaussian Example

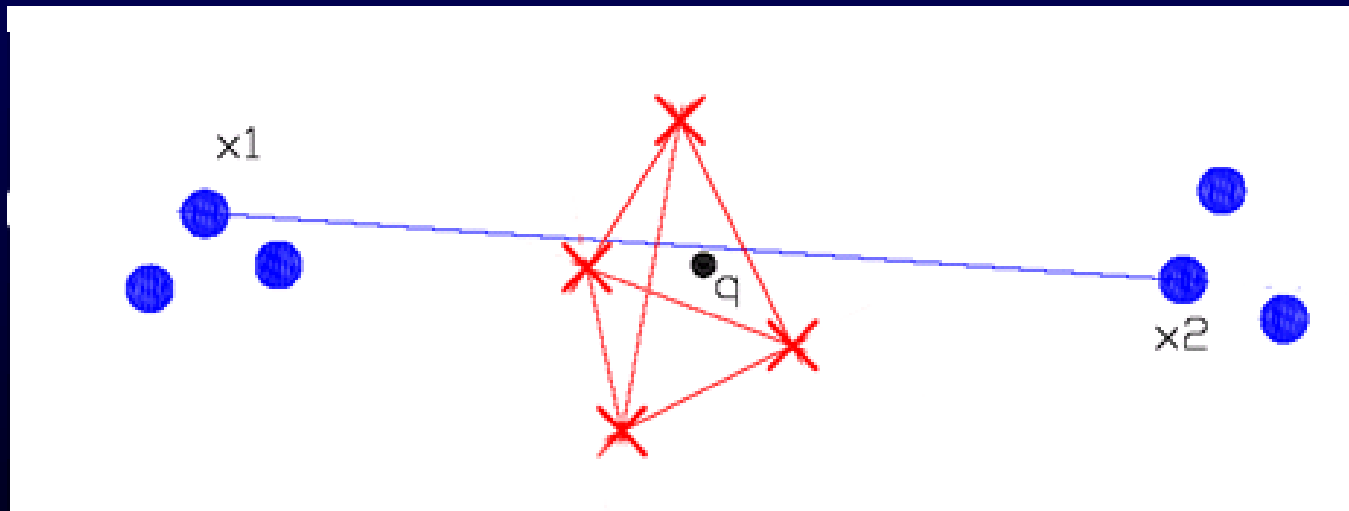
- Sample distribution is centralized by NFL-Segment



- Correct-classification-rate increases
  - 82% -> 86%

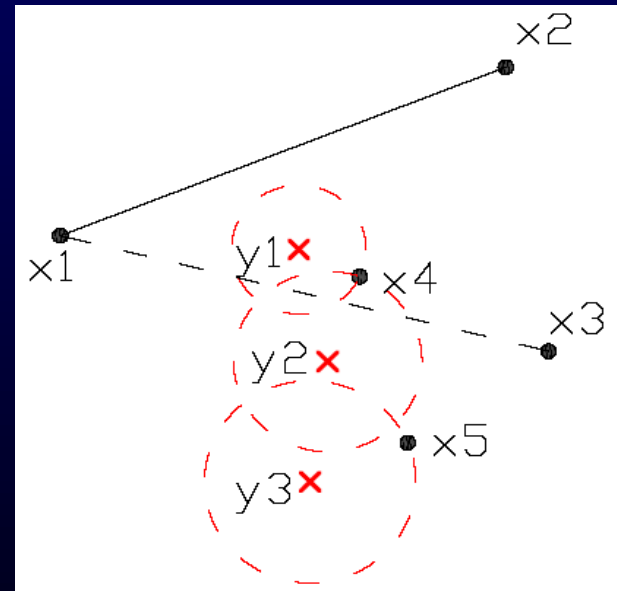
# What if multi-center distribution?

- ④ Problem:
  - ⊗ Feature lines of one class may trespass other class area, causing decision errors



# Rectified NFL-Segment

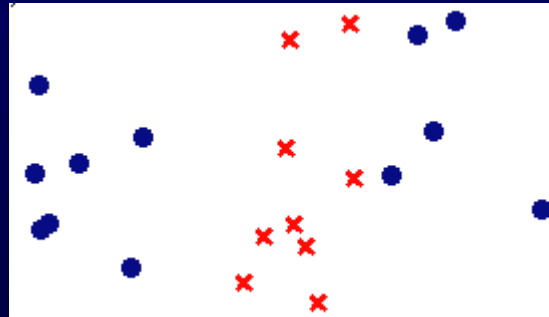
- ④ Idea : remove all the feature lines trespassing the territory of other classes
- ④ Territory
  - ⊗ sample-territory
  - ⊗ class-territory



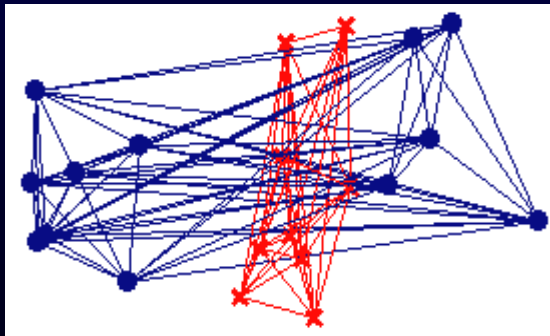
As shown in the picture, feature line segment  $X_1X_3$  will be removed for it trespasses the territory of class “cross”

# Review the whole process

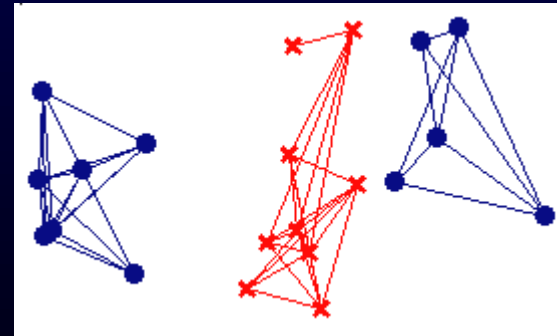
- ② Density Functions are centralized in different areas



(a) Nearest Neighbor



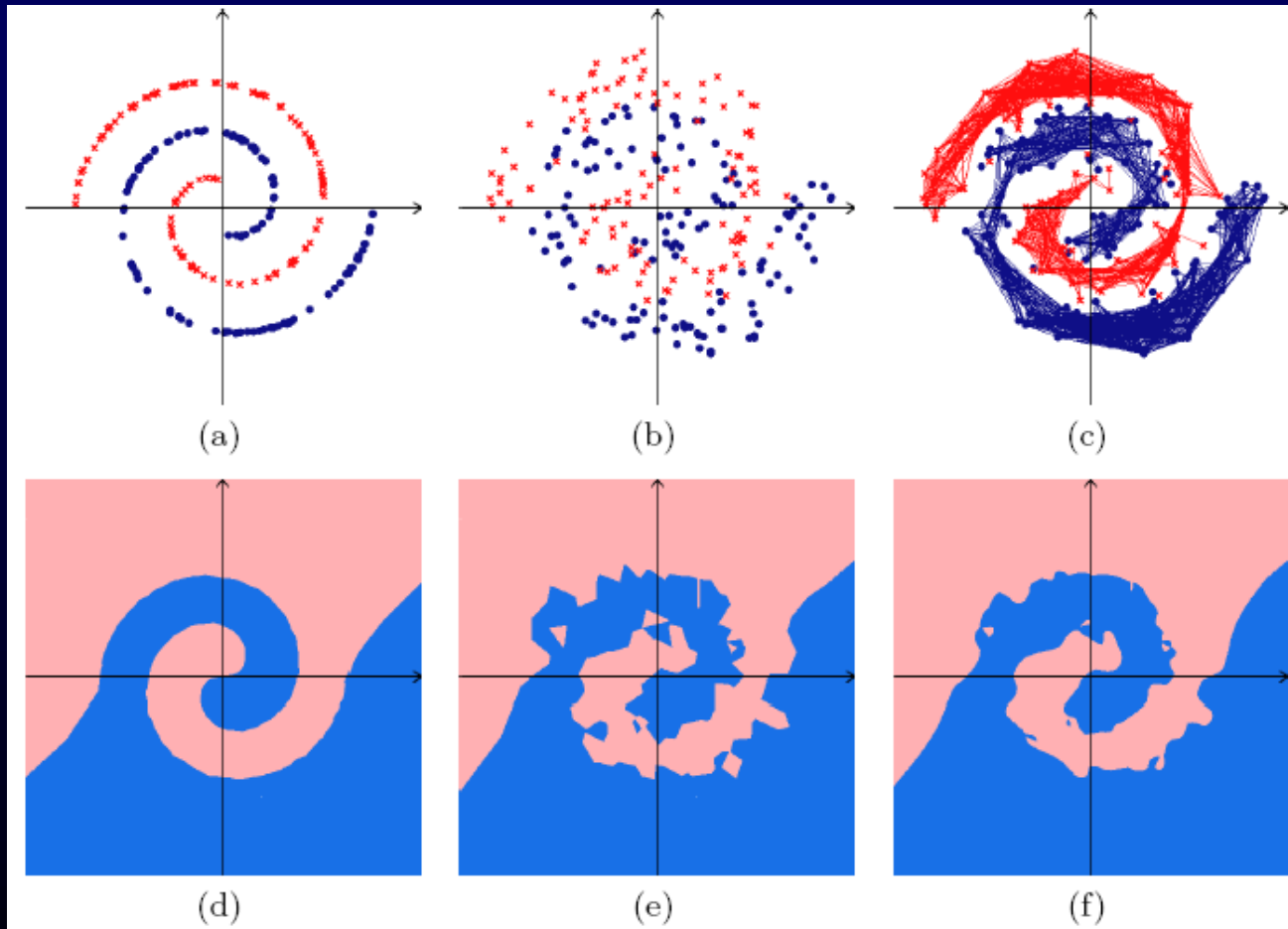
(b) NFL-Segment



(c) Rectified-NFL-Segment

# Two-spiral Experiments

- Centralization property helps to optimize the decision region



# Experiments: UCI-datasets

- Real-World Problems
  - UCI datasets
  - CCR(%) by leave-one-out procedure

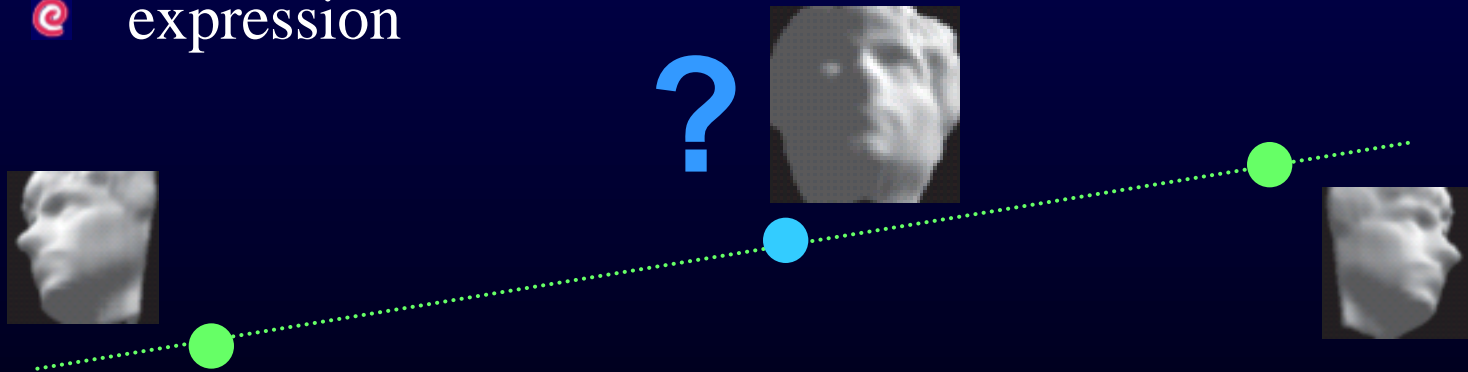
	Dataset	#Classes	#Instances	#Attributes	NN	3NN	NFL	NNL	RNFLS
1	hepatitis	2	80	19	<b>92.5</b>	91.3	91.3	76.3	91.3
2	iris	3	150	4	94.7	94.7	88.7	94.7	<b>95.3</b>
3	housing	6	506	13	70.8	73.0	71.1	67.6	<b>73.5</b>
4	pima	2	768	8	70.6	<b>73.6</b>	67.1	62.8	73.0
5	wine	3	178	13	95.5	95.5	92.7	78.7	<b>97.2</b>
6	bupa	2	345	6	63.2	65.2	63.5	57.4	<b>66.4</b>
7	ionosphere	2	351	34	86.3	84.6	85.2	87.2	<b>94.3</b>
8	wpbc	2	194	32	72.7	68.6	72.7	54.1	<b>75.8</b>
9	wdbc	2	569	30	95.1	96.5	95.3	64.0	<b>97.2</b>
10	glass	6	214	9	70.1	72.0	66.8	65.4	<b>72.0</b>

# Interesting property of Feature Line(1/3)

## ④ S.Z. Li (1999), Nearest Feature Line:

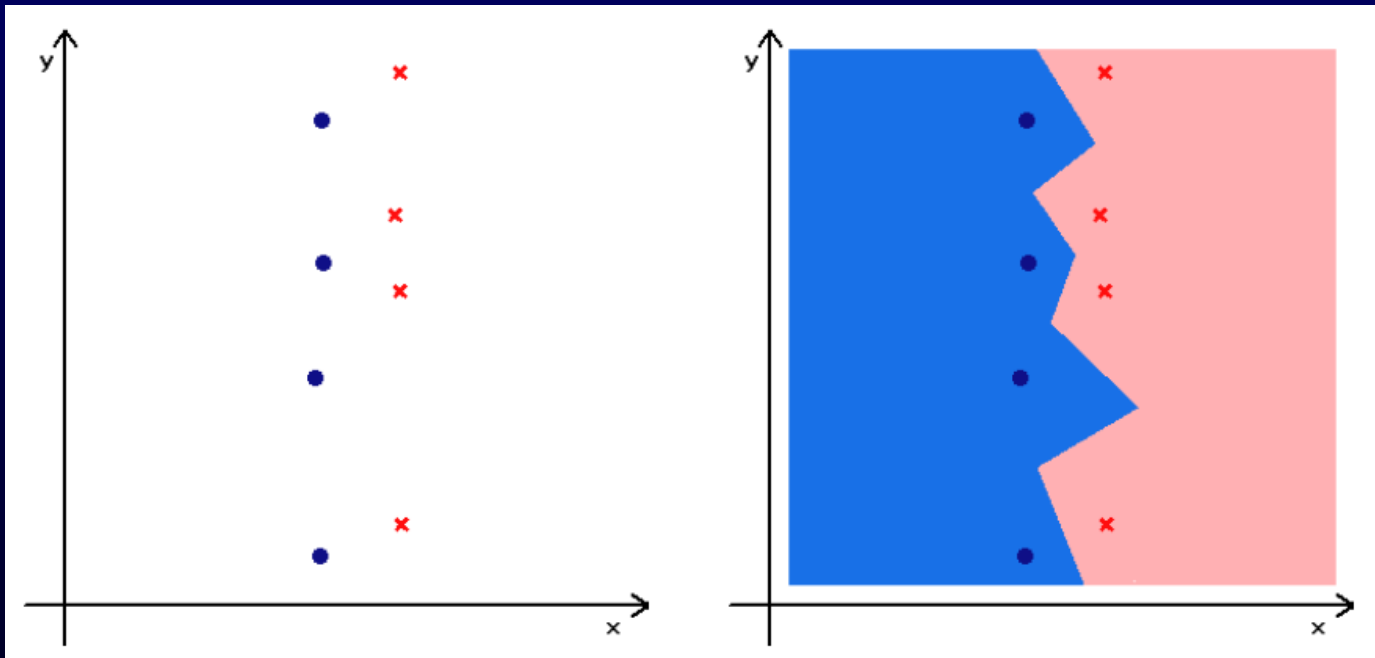
In Face-Recognition problem, Feature Line linearly expand two prototypes, approximating variants of two prototypes in

- ④ pose
- ④ illumination
- ④ expression



# Interesting property of Feature Line(2/3)

④ Another example:



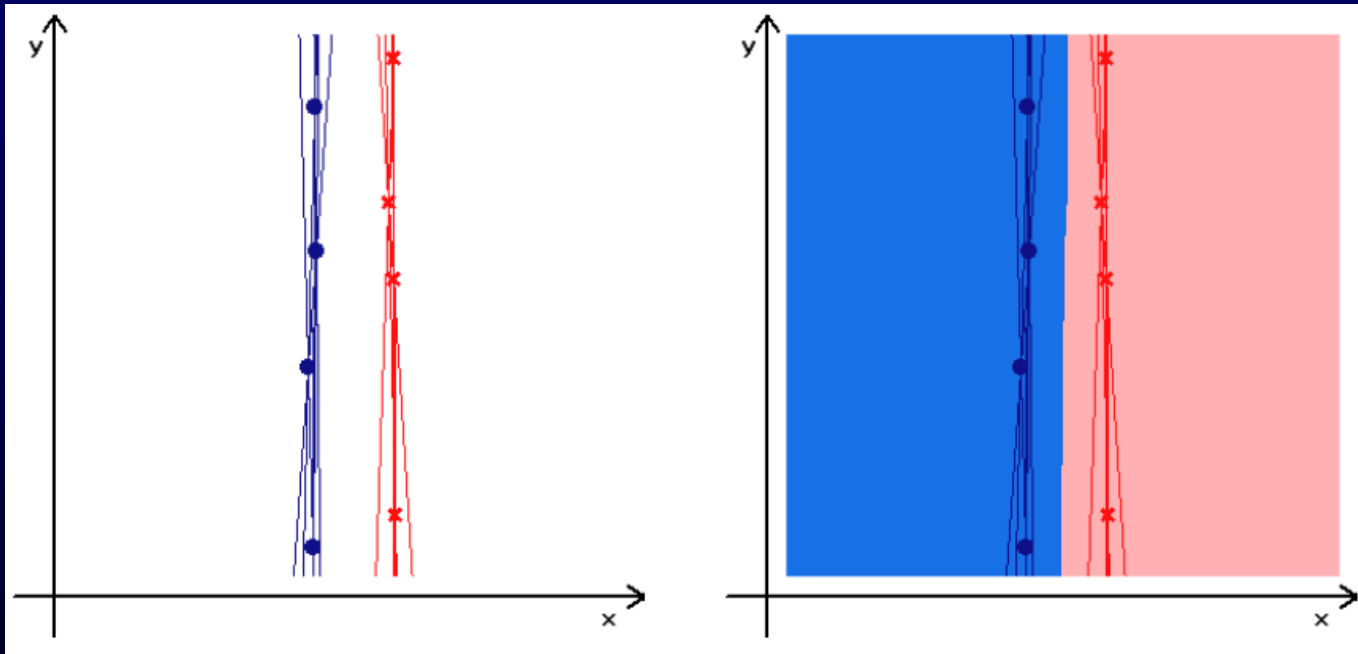
(a) Original Samples

(b) Decision Region by NN



# Interesting property of Feature Line(3/3)

② Another example:



(c) Feature Lines

(d) Decision Region by NFL

@ Q & A

**Thank you!**